

CHANGE OF FORCE BETWEEN SHAFTS AND WINDING PITCH RADIUS OF CHAIN TYPE CONTINUOUSLY VARIABLE TRANSMISSION AT STEADY STATE

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Abstract

The objective of this study is to clarify the mechanism for changing the force between driving and driven shaft and winding pitch radius of a chain type Continuously Variable Transmission at nominal steady state. Nonlinear decrease and nonlinear increase of the pitch radius of the chain belt were observed at the entrance and exit, respectively, due to the tilt of movable sheave. This study found that the force between shafts was changed by the change of total reaction forces in contraction direction, where contact region between chain belt and pulley was also changed.

Keywords

Chain belt; CVT (Continuously Variable Transmission); Force between shafts; Power transmission

Introduction

Continuously Variable Transmissions (CVTs) are widely used as an automobile transmission for passenger cars since they provide comfortable driving by adjusting the speed ratio continuously. A lot of researches have focused on CVTs to further improve performance of automobiles [1-6]. The transmitting torque is estimated by the classical theory with force between shafts for the belt transmission mechanism [7]. It is considered that the force between shafts of chain type CVTs is the important parameter to determine their performance. Force between shafts is changed with respect to applied torque when the pulley thrust is constant. Winding pitch radius of belt is also changed with respect to applied torque at steady state [8]. However, the behaviors represented with force between shafts and winding pitch radius were not simply estimated by the classical theory. The objective of this study is to clarify the mechanism for changing force between driving and driven shaft and winding pitch radius of chain type CVTs at steady state. In this study, two types of pulleys (movable pulley and fixed pulley) were prepared to investigate the influence of the tilt of pulley on the mechanical behavior of chain type CVTs.

Test method

Testing System

(Figure 1) shows the illustration of our original testing system. The generated mechanical power on AC motor was transmitted from driving axis to driven axis through the CVT unit. The rotational speed and transmitting torque were simultaneously measured by conventional tachometers and torque meters, respectively. Driven torque was applied by rotational frictional disc brake. Pulley thrust force was also applied to a chain belt by the oil pressure. CVT fluid was circulated to prevent wear of a chain belt and pulleys during transmission. In addition, the driving pulley unit was set on the linear rail, and connected to load cell. The force between shafts was measured by the load cell during experiment.
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Where, \( N_{\text{DR}} \) and \( N_{\text{DN}} \) denote the rotational speed of the driving axis and that of the driven axis, respectively. The speed ratio \( i \) without loading torque was set to 2.48. The pulley thrust of the driven pulley \( Q_{\text{DN}} \) was kept constant at 60kN, while the driving torque \( T_{\text{DR}} \) was steadily increased from 0 Nm up to the state of sliding slip. The movable sheave of driving pulley was supported with the pulley-stopper.

<table>
<thead>
<tr>
<th>Code</th>
<th>Driving pulley</th>
<th>Driven pulley</th>
</tr>
</thead>
<tbody>
<tr>
<td>M-M</td>
<td>Movable</td>
<td>Movable</td>
</tr>
<tr>
<td>F-M</td>
<td>Fixed</td>
<td>Movable</td>
</tr>
</tbody>
</table>

Table 1: Test codes of combinations of driving and driven pulley.

Measurements of Force Between Shafts

(Table 2) shows the test conditions for this test. The rotational speed of the driving pulley \( N_{\text{DR}} \) was kept constant at 600rpm during experiments. Speed ratio was defined as equation (1).

\[
i = \frac{N_{\text{DR}}}{N_{\text{DN}}}
\]  
(1)

| Driving rotational speed \( N_{\text{DR}} \) [rpm] | 600 |
| Pulley thrust of driven pulley \( Q_{\text{DN}} \) [kN] | 60 |
| Oil pressure of driving pulley \( P_{\text{DR}} \) [MPa] | 0 |
| Speed ratio \( i_0 \) [-] (Without loading torque) | 2.48 |
| Driving torque \( T_{\text{DR}} \) [Nm] | \( \sim \) sliding slip |

Table 2: Test conditions for measurements of force between shafts.

Measurements of Change of Observed Wedge Angle and Radial Displacement

(Table 3) shows the test conditions for these tests. The change of observed wedge angle of movable sheave of driving pulley and the radial displacement of chain belt were measured by laser displacement sensors. The rotational speed of the driving pulley \( N_{\text{DR}} \) was kept constant at 200 rpm during experiments.

| Driving rotational speed \( N_{\text{DR}} \) [rpm] | 200 |
| Pulley thrust of driven pulley \( Q_{\text{DN}} \) [kN] | 60 |
| Oil pressure of driving pulley \( P_{\text{DR}} \) [MPa] | 0 |
| Speed ratio \( i_0 \) [-] (Without loading torque) | 2.48 |
| Driving torque \( T_{\text{DR}} \) [Nm] | \( \sim \) sliding slip |

Table 3: Test conditions for measurements of change of observed wedge angle and radial displacement.

Measurements of Strains on Rocker Pin

Strains on the rocker pin were investigated by strain gauges. Strain gauges were set on both surfaces of the rocker pin as shown in (Figure 3). Test conditions were followed as same with those on (Table 3). Compressive strain \( \varepsilon_C \) was calculated by equation (2) to cancel the bending strain.

\[
\varepsilon_C = \frac{\varepsilon_1 + \varepsilon_2}{2}
\]  
(2)

Where, \( \varepsilon_1 \) and \( \varepsilon_2 \) denote strains on each surface.
Results and discussions

Force Between Shafts $F_s$

(Figure 4) shows the change of the force between shafts $F_s$ with respect to driving torque $T_{DR}$. The force between shafts $F_s$ was decreased about 10% just before the state of sliding slip compared to that at the maximum under the M-M condition. It was found that the force $F_s$ was relatively large when the sliding motion of the driving pulley was fixed.

Radial Displacement of Chain Belt $\Delta R$

(Figure 5) shows the radial displacement of chain belt $\Delta R$ with respect to driving torque $T_{DR}$ near the entrance and exit of the driving pulley when the movable pulleys were applied to the both of driving and driven pulley. The radial displacement of chain belt $\Delta R$ was decreased nonlinearly near the entrance, while that was increased nonlinearly near the exit, when the driving torque was increased. (Figure 6) also shows the change of observed wedge angle of movable sheave of the driving pulley $\Delta \theta$ with respect to the driving torque $T_{DR}$. Near the entrance of the driving pulley, the observed wedge angle was increased nonlinearly, while near the exit, that was decreased nonlinearly. (Figure 7) shows the relation between radial displacement of chain belt $\Delta R$ and the change of observed wedge angle of movable sheave $\Delta \theta$. The correlation between the radial displacement and the change of observed wedge angle of movable sheave $\Delta \theta$ was found.
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Figure 7: Radial displacement $\Delta R$ with respect to change of observed wedge angle $\Delta \theta$.

To discuss the results, the radial displacement due to the tilt of movable sheave $\Delta R_{\text{tilt}}$ was estimated with geometrical relationship by equation (3).

\[
\Delta R_{\text{tilt}} = R \left\{ \frac{\tan \left( \frac{\alpha}{2} \right)}{\frac{\tan \left( \frac{\alpha}{2} + \Delta \theta \right)}{1}} - 1 \right\} \tag{3}
\]

Where, $\alpha$ and $R$ denote the wedge angle of the movable sheave, and the winding radius of chain belt, respectively. (Figure 8) shows the measured and calculated radial displacements due to the tilt of the movable sheave $\Delta R_{\text{tilt}}$ with respect to driving torque $T_{\text{DR}}$. It was found that the estimated results of the radial displacements were agreed well with those of experimental data, when the tilt of movable sheave was considered. It was shown that the radial displacement $\Delta R$ was dominated by the change of observed wedge angle of the movable sheave $\Delta \theta$.

Figure 8: Radial displacements $\Delta R$ due to tilt of movable sheave.

Change of Contact Region Between Rocker Pins And Pulley in Driving Pulley Groove

(Figure 9) shows the change of compressive strain on the rocker pin with respect to the non-dimensional location of the rocker pin, when the driving torque $T_{\text{DR}}$ was 100 Nm, where, non-dimensional location was defined as the passing distance divided by the belt length for a circulation. (Figure 10) also shows the magnified graph focusing on the data in driving pulley groove shown on the last graph. Effective contact region between rocker pins and pulley was defined as the length from the first peak of the compressive strain to the second peak in the driving pulley. The $L_{\text{M-M}}$ and $L_{\text{F-M}}$ denote the effective contact region of M-M condition and that of F-M condition, respectively. It was found that the effective contact region was decreased when the movable pulleys were applied to the both of driving and driven pulley.

Figure 9: Example data of change of compressive strains on rocker pin.

Figure 10: Change of contact regions between rocker pins and pulley in driving pulley groove.
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(Figure 11) shows the change of decreasing ratio of the contact region with respect to the driving torque $T_{DR}$. Decreasing ratio of contact region $\Delta \beta$ was defined as the relative difference between contact region of M-M condition and that of F-M condition. The decreasing ratio of contact region was estimated by equation (4).

$$\Delta \beta = C \cdot T_{DR} \quad (4)$$

Where, $C=4.0 \times 10^{-4} \, [/(Nm)]$, which was determined by experiments.

![Figure 11: Change of decreasing ratio of contact region $\Delta \beta$ with respect to driving torque $T_{DR}$](image)

The change of force between shafts $\Delta F_S$ is also calculated by considering the change of wrapping angle and contact region by equation (5).

$$\Delta F_S = F_{S0}(1 - \cos(\theta_0 \Delta \beta)) \quad (5)$$

Where, $F_{S0}$ and $\theta_0$ denote the force between shafts in case that the fixed pulley was applied to the driving pulley, and wrapping angle of driving pulley, respectively. (Figure 12) shows the change of the force between shafts $\Delta F_S$ with respect to driving torque $T_{DR}$, where experimental data of $\Delta F_S$ were determined by calculating the data shown in figure 4. The triangle plots and solid line in the figure represent the measured data and the estimated data by equation (5), respectively. The estimated result was agree well with the experimental data. By the results, it was suggested that the force between shafts $F_S$ was changed by the change of total reaction forces in the contraction direction, where the contact region between the chain belt and the pulley was also changed.

![Figure 12: Change of force between shafts $\Delta F_S$ with respect to driving torque $T_{DR}$](image)

Conclusion

1. Comparatively large force between shafts was measured when the sliding motion of the driving pulley was fixed.
2. It was shown that the radial displacement of the chain belt was dominated by the change of observed wedge angle of the driving pulley.
3. It was suggested that the force between shafts was changed by the change of total of reaction forces in the contraction direction, where the contact region between the chain belt and the pulley was also changed.

References


